

Supporting Information for

Na/Ca Intermixing around Silicate and Phosphate Groups in Bioactive Phosphosilicate Glasses Revealed by Heteronuclear Solid-State NMR and Molecular Dynamics Simulations

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S1 Experimental and Numerical Procedures

S1.1 MD Simulations

The MD simulation procedures followed those outlined in our previous work.^{S1–S3} Except for the glass models of the CaO–SiO₂ and Na₂O–SiO₂–P₂O₅ glasses presented herein, the parameters utilized for all simulations of the Na₂O–CaO–SiO₂–P₂O₅ glasses were discussed by Stevansson *et al.*^{S2} **Table S2** lists the number of simulated atoms, box dimensions, as well as the number of independent simulations performed for each glass composition.

The polarizable shell-model potential utilized cations carrying their full formal charges, whereas the O²⁻ species were represented by core (O_C) and shell (O_S) units with charges of $z_C = +0.8482e$ and $z_S = -2.8482e$, respectively, implying $z_C + z_S = -2$.^{S4} They were coupled by a 300 THz harmonic oscillator. A Buckingham potential accounted for all short-range O_S–O_S and cation–O_S pair interactions [using the parameters of refs. (S5–S7)], which were evaluated out to 0.8 nm.^{S4} Long-range Coulombic interactions were calculated by a smoothed particle mesh Ewald summation^{S8} with a 1.2 nm real-space cut-off and an accuracy of 10⁻⁶. The O–Si–O and O–P–O intratetrahedral angles were constrained with three-body truncated harmonic potentials.^{S8} The equations of motion were integrated in steps of 0.2 fs using the velocity Verlet integrator, while the temperature was controlled by a Berendsen thermostat associated with a 1.0 ps time constant.

S1.2 Heteronuclear NMR Experimentation

Here we provide the experimental details of the heteronuclear ²³Na↔²⁹Si and ²³Na↔³¹P NMR experimentation. For the ²³Na–³¹P pair, $M_2(\text{P–Na})$ and $M_2(\text{Na–P})$ data were reported by Stevansson *et al.*^{S3} for several BG_p^q($\overline{N}_{\text{BO}}^{\text{Si}}$) samples. Ref. (S3) reported a straightforward $M_2(\text{S–I})\leftrightarrow M_2(\text{I–S})$ conversion protocol (demonstrated on the ²³Na–³¹P pair in phosphosilicate glasses), whereas the present study discusses the implications for composition/structure correlations, as well as presenting new data from additional glass specimens.

All ²³Na{³¹P} REDOR and ³¹P{²³Na} REAPDOR NMR data discussed in the main text were recorded at 9.4 T and 14.000 kHz MAS with a Bruker Avance-III spectrometer and a 4 mm triple-resonance (TR) MAS probehead. The spinning rate was stable within ±2 Hz throughout. All recoupling experiments involved central-transition (CT) selective ²³Na pulses operating at $\nu_1^{\text{Na,CT}} \approx 16.0$ kHz, corresponding to 90°/180° pulse-lengths of 15.6/31.3 μs. The ³¹P/²⁹Si 180° recoupling pulses were 6.9/8.0 μs for both REDOR and REAPDOR NMR acquisitions, with the rf phases cycled according to XY16 scheme^{S9} to minimize radio-frequency (rf) errors. The dipolar dephasing data was sampled at *even integral* multiples of the rotational period τ_r . The REAPDOR experiments started from directly excited ³¹P/²⁹Si magnetization by application of a 90° pulse. The adiabatic-passage pulse for REAPDOR operated at $\nu_1^{\text{Na}} = 75$ kHz for 24 μs (i.e., $\tau_r/3$). Saturation-recovery blocks were used prior to relaxation delays of 20 s and 200 s in the recording of each ³¹P{²³Na} and ²⁹Si{²³Na} REAPDOR signal transient, respectively, whereas those for ²³Na{³¹P} and ²³Na{²⁹Si} REDOR employed 4 s. All REDOR experimentation utilized the RAPT technique^{S10} to enhance the ²³Na CT magnetization and thereby the experimental sensitivity, where typically 40 pulse-blocks were employed with equal pulse/interpulse durations of 0.55 μs and $\nu_1^{\text{Na}} = 75$ kHz.

The REDOR/REAPDOR NMR data were acquired in 3–4 blocks per phosphosilicate sample, each involving 16–64 accumulated signal transients, depending on the particular experimental protocol and glass composition. These independent experimental data sets were separately processed, integrated, and numerically fitted to eq. (2), as discussed in detail in the **SI** of Stevansson *et al.*^{S3} Note that all heteronuclear NMR experimentation involved full rotors. The presence of rf

inhomogeneity is known to give underestimated dipolar-derived structural data.^{S11,S12} **Table S4** reports the resulting average dipolar second moments and their associated uncertainties, as obtained from the blocks of independently acquired experimental data. All experiments were performed at 25 °C. To verify if Na mobility could affect the dipolar dephasing, we also performed $^{29}\text{Si}\{^{23}\text{Na}\}$ REAPDOR experiments at -80 °C on the $\text{BG}_{6.0}^{1.00}(2.5)$ specimen, however, without observing any significant difference.

Note that computer modeling was used exclusively to probe the Ca–Si/P spatial proximities, owing to the very low natural abundance (0.15%) and substantial costs of the ^{43}Ca isotope ($S=7/2$), coupled with its low NMR signal-sensitivity even for enriched specimens.

S2 The Relative Dephasing for $^{29}\text{Si}\longleftrightarrow^{23}\text{Na}$ and $^{31}\text{P}\longleftrightarrow^{23}\text{Na}$ in RE-DOR/REAPDOR NMR

It is instructive to compare the different time-scales over which the $^{23}\text{Na}\longleftrightarrow^{31}\text{P}$ and $^{23}\text{Na}\longleftrightarrow^{29}\text{Si}$ experiments dephase in Figs. 4 and 6 in relation to both the Si and P contents of the BG and the very different sizes of the magnetogyric ratios ($\gamma_{\text{Si}} = -5.3 \cdot 10^7 \text{ rads}^{-1}\text{T}^{-1}$; $\gamma_{\text{P}} = 10.8 \cdot 10^7 \text{ rads}^{-1}\text{T}^{-1}$) that together with the common factor $\gamma_{\text{Na}} = 7.1 \cdot 10^7 \text{ rads}^{-1}\text{T}^{-1}$ for ^{23}Na enter the expressions for the respective dipolar coupling constants $b_{\text{Na-Si}}$ and $b_{\text{Na-P}}$. The ratio $|\gamma_{\text{P}}/\gamma_{\text{Si}}| \approx 2$ implies that if the number-densities of ^{29}Si and ^{31}P would be identical in the glass (note that $r_{\text{Si-Na}} \approx r_{\text{P-Na}}$), the stronger $^{23}\text{Na}\text{--}^{31}\text{P}$ dipolar contacts themselves should lead to roughly $(\gamma_{\text{P}}/\gamma_{\text{Si}})^2 \approx 4$ times faster $^{23}\text{Na}\{^{31}\text{P}\}$ REDOR dephasing compared to its $^{23}\text{Na}\{^{29}\text{Si}\}$ counterpart [see eq. (1)]. Yet, the significantly higher Si content relative to that of P in the present glasses counterbalance the effect of the larger γ_{P} value: this yields a comparable $^{23}\text{Na}\{^{29}\text{Si}\}$ dephasing for the ^{29}Si -enriched $\text{BG}_{6.0}^{0.43}(2.5)$ and $\text{BG}_{6.0}^{1.00}(2.5)$ glasses [Fig. 6(a)] relative to that of the $^{23}\text{Na}\{^{31}\text{P}\}$ REDOR scenario shown in Fig. 4(a). For the REAPDOR experimentation, on the other hand, where all concentration effects of the *observed* ^{31}P of ^{29}Si species are eliminated [see eq. (1)], the consequences from the widely differing magnetogyric ratios (γ_{P} and γ_{Si}) become evident; they account for the markedly slower $^{29}\text{Si}\{^{23}\text{Na}\}$ REAPDOR dynamics observed in Fig. 6 compared with the $^{31}\text{P}\{^{23}\text{Na}\}$ counterpart in Fig. 4. The relative dephasing trends among the $^{29}\text{Si}/^{23}\text{Na}$ and $^{31}\text{P}/^{23}\text{Na}$ pairs of nuclei are mirrored in the respective NMR/MD-derived second moments listed in **Table S4**, where $M_2(\text{Na-P})$ and $M_2(\text{Na-Si})$ reveal similarly-sized values, whereas the $M_2(\text{P-Na})$ data are almost an order of magnitude larger than those of $M_2(\text{Si-Na})$.

The slower dipolar recoupling dynamics of the $^{29}\text{Si}\{^{23}\text{Na}\}$ REAPDOR experimentation and its concurrent accumulation of rf-pulse errors account for the strongly non-ideal dephasing behavior observed beyond a few ms; note that in the case of REAPDOR, the train of 180° pulses is applied to the *observed* ^{29}Si spins (see Fig. S1). Moreover, the REAPDOR technique is well-known to be very susceptible to MAS-rate fluctuations.^{S13,S14} The best-fit $M_2(\text{Si-Na})$ value from the mixed-modifier glass $\text{BG}_{6.0}^{0.43}(2.5)$ accorded very well with that obtained by MD simulations. In contrast, the second moment measured directly by $^{29}\text{Si}\{^{23}\text{Na}\}$ REAPDOR from the Na–Si–P–O glass $\text{BG}_{6.0}^{1.00}(2.5)$ is significantly lower than its modeled counterpart, while that determined indirectly by converting the corresponding $^{23}\text{Na}\{^{29}\text{Si}\}$ REDOR-derived result accorded well with the MD result. We have no satisfactory explanation for these observations, but we note that Na mobility (which is well-known to affect dipolar-coupling-based experiments) is unlikely to be the reason, given that no significant differences were observed in the $^{29}\text{Si}\{^{23}\text{Na}\}$ NMR signal dephasing between experiments performed at room temperature and at -80 °C under otherwise identical conditions.

S3 Prediction of Z_{tot}^T for each Q_{Si}^n and Q_{P}^n Group

The MD-derived total coordination number $Z_{\text{tot}}(Q_T^n) \equiv Z(Q_T^n\text{-Na}) + Z(Q_T^n\text{-Ca})$ of each Q_T^n moiety depends foremost on the total number density of the modifier ions, $\rho(M_{\text{tot}})$. For the phosphate species, good fits were obtained by using this parameter alone,

$$Z_{\text{tot}}(Q_{\text{P}}^0) = 6.0281 + 0.1992\rho(M_{\text{tot}}), \quad R^2 = 0.970, \quad (\text{S1})$$

$$Z_{\text{tot}}(Q_{\text{P}}^1) = 3.8893 + 0.2259\rho(M_{\text{tot}}), \quad R^2 = 0.965, \quad (\text{S2})$$

whereas the coordination numbers of each Q_{Si}^n species generally also depended on the P content (i.e., ρ_{P}), as follows:

$$Z_{\text{tot}}(Q_{\text{Si}}^1) = 5.7693 + 0.1741\rho(M_{\text{tot}}), \quad R^2 = 0.928, \quad (\text{S3})$$

$$Z_{\text{tot}}(Q_{\text{Si}}^2) = 3.3472 + 0.2219\rho(M_{\text{tot}}) - 0.0617\rho_{\text{P}}, \quad R^2 = 0.996, \quad (\text{S4})$$

$$Z_{\text{tot}}(Q_{\text{Si}}^3) = 1.1667 + 0.2495\rho(M_{\text{tot}}) - 0.0853\rho_{\text{P}}, \quad R^2 = 0.998, \quad (\text{S5})$$

$$Z_{\text{tot}}(Q_{\text{Si}}^4) = -0.7018 + 0.2471\rho(M_{\text{tot}}), \quad R^2 = 0.962. \quad (\text{S6})$$

Note that the best-fit coefficient for ρ_{P} is zero for the Q_{Si}^1 groups (i.e., $Z_{\text{tot}}(Q_{\text{Si}}^1)$ is independent on ρ_{P}), while *negative* coefficients are observed in the expressions for the Q_{Si}^2 and Q_{Si}^3 groups, where the *magnitude* of the coefficient increases together with the number of BO atoms (n) at the Q_{Si}^n tetrahedron. This trend reflects that the most negatively charged Q_{Si}^1 groups ($\text{SiO}_{3.5}^{3-}$) control their own coordination shells to a larger extent than their Q_{Si}^2 (SiO_3^{2-}) and Q_{Si}^3 ($\text{SiO}_{2.5}^{-}$) counterparts. Hence, the coordination numbers of the Q_{Si}^2 and Q_{Si}^3 groups *reduces* when the P content of the glass is increased, because the higher negative charge of the Q_{P}^0 (PO_4^{3-}) unit attract the $\text{Na}^+/\text{Ca}^{2+}$ cations more efficiently. In contrast, the formally *uncharged* Q_{Si}^4 groups also give an exception in that $Z_{\text{tot}}(Q_{\text{Si}}^4)$ is also independent on ρ_{P} . The reason is likely their *overall* low affinity for the modifiers.

Figure **S3** plots the correlation between the MD-derived coordination number and its best-fit counterpart calculated from eqs. (S1)–(S6) for each Q_T^n group. The agreement is very good throughout, as reflected in the near-unity correlation coefficients ($R^2 \approx 1$). The largest deviations ($R^2 = 0.928$) are observed for $Z_{\text{tot}}(Q_{\text{Si}}^1)$. Note, however, that no quality-improvement of the fit [eq. (S3)] resulted when also invoking ρ_{P} as an independent parameter in the numerical fitting ($R^2 = 0.921$).

S4 Contributions from the First Coordination Shell $Q_T^n\text{-}M$ Contacts to $M_2(Q_T^n\text{-}M)$

Table S6 reveals that the Si/P–Na/Ca contacts in the first coordination shell of each Q_T^n group generally contributes to 80–90% of the (converged) $M_2(Q_T^n\text{-}Na)$ and $M_2(Q_T^n\text{-}Ca)$ second moments. Noteworthy, these fractions are almost equal for Na and Ca and essentially independent on the glass composition, meaning that the conclusions about the relative $T\text{-}Na$ and $T\text{-}Ca$ preferences drawn from the $\{Z_{\text{Na}}^T, Z_{\text{Ca}}^T\}$ pair are fully representative also for the longer-range contacts. The only exceptions are the lower-charged silicate groups: the $\text{Na}^+/\text{Ca}^{2+}$ cations of the first coordination shell for Q_{Si}^3 accounts for 81% (Na) and 73% (Ca) out of the respective total $M_2(Q_{\text{Si}}^3\text{-}M)$ values, whereas the Q_{Si}^4 groups reveal much lower fractions of $\approx 73\%$ and $\approx 39\%$ for Na and Ca, respectively (see **Table S6**). Consequently, assessments made from $\{Z_{\text{Na}}^T, Z_{\text{Ca}}^T\}$ data of these silicate groups tend

to overestimate their preferences for Na contacts; only slightly for the Q_{Si}^3 moieties, but substantially for Q_{Si}^4 . These effects are apparent in the $R_{\text{Na/Ca}}(Q_{\text{Si}}^n)$ factors listed in **Table S5**, whose values derived by requiring that Si and Na/Ca share O atoms (and thereby share first coordination shells) are larger than the $R_{\text{Na/Ca}}(Q_T^n)$ counterpart evaluated out to $r=450$ pm. We stress, however, that the deviations among the two $R_{\text{Na/Ca}}(Q_T^n)$ sets are insignificant for all other Q_T^n species, which consistently reveal values well within the data uncertainties.

S5 Limitations of Heteronuclear and ^{17}O NMR Experimentation

While the experimental/numerical errors of the NMR/MD-stemming $M_2(\text{P-Na})$ values are generally within the symbol sizes in Figs. **5** and **10(a)**, and the error bars of the various $\{P_{\text{Ca}}\}$ estimates in Fig. **10(b)** do generally not overlap, the *spread* among the two independent experimental datasets better conveys the accuracy limited by *systematic* errors of this type of heteronuclear NMR implementations. As discussed further in refs. (S2,S3), $M_2(\text{S-I})$ data from glasses are prone to be *underestimated* due to rf inhomogeneity, the presence of paramagnetic doping, and the approximations inherent to eq. (2) used for fitting. Note that the second moments of Figs. **5** and **10** were already corrected for most of these systematic errors; if the same analysis is applied to the *uncorrected* REAPDOR-stemming data,^{S3} significantly higher P_{Ca} -values between 0.33–0.46 results.

Furthermore, given that we are quantifying a degree of preference for Ca (i.e., P_{Ca}) from information about $M_2(\text{P-Na})$, *any underestimate in $M_2(\text{P-Na})$ translates into an overestimate of P_{Ca}* . This property follows from eqs. (6) and (7) and that only the factor P_M of the *preferred* cation M is well-defined (i.e., there is no exact relationship between P_M and $P_{M'}$). An independent measurement of $M_2(\text{P-Ca})$ is unfortunately intractable (see **section S1.2**), but such values are *also* expected to be underestimated, thereby leading to an *underestimation* of P_{Ca} . Thus, access to *both* independent $M_2(\text{P-Ca})$ and $M_2(\text{P-Na})$ results would provide both upper/lower limits of the P_{Ca} estimate. Moreover, the $M_2(Q_{\text{P}}^0\text{-Na})$ values calculated from the $\{P_M, Z_{\text{tot}}^T(Q_T^n), \bar{r}_{T-M}\}$ parameters are inherently biased to the MD-generated structural data from which they were derived. Higher experimental P_{Ca} parameters are therefore anticipated from the *lower* experimental $M_2(\text{P-Na})$ data relative to the simulated ones (Fig. **5**). The gray region around $P_{\text{Ca}}=P_{\text{Na}}=0$ in Fig. **10(a)** illustrates the spread in $M_2(Q_{\text{P}}^0\text{-Na})$ resulting solely when $Z_{\text{tot}}(Q_{\text{P}}^0)$ is varied by ± 1 (i.e., by $\approx 10\%$).

After the critical remarks on the present data, we note that our conclusions about modifier (dis)ordering in glasses are both more transparent and precise than previous assessments by similar heteronuclear recoupling experimentation applied to other glass systems/nuclei, where the conclusions from the second-moment data were of more qualitative nature.^{S15–S22} Moreover, earlier inferences about cation intermixing around silicate groups by ^{17}O NMR^{S23–S25} are plagued by similar problems as the heteronuclear NMR experimentation: limited spectral resolution with overlap among the ^{17}O resonances from distinct BO/NBO- M/M' contacts and assumptions required about the total coordination number of modifiers at the O sites may together produce significant systematic errors in the subsequent NMR peak-deconvolution into several peaks of *a priori* unknown positions and widths.

Table S1: Fractional Populations of Q_P^n and Q_{Si}^n Groups^a

glass	P		Si				silicate network connectivity		
	x_P^0	x_P^1	x_{Si}^1	x_{Si}^2	x_{Si}^3	x_{Si}^4	$\overline{N}_{BO}^{Si}(\text{nom})$	$\overline{N}_{BO}^{Si}(\text{NMR})$	$\overline{N}_{BO}^{Si}(\text{MD})$
BG ₀ ⁰ (2.0)	–	–	0.168(0.243)	0.745(0.472)	0.087(0.241)	0.000(0.022)	2.00	1.92	2.00
BG _{2,6} ^{0.48} (2.1)	0.959(0.834)	0.041(0.166)	0.066(0.186)	0.724(0.517)	0.210(0.266)	0.000(0.021)	2.11	2.14	2.10
BG _{6,0} ^{0.41} (2.1)	0.955(0.798)	0.045(0.200)	0.056(0.197)	0.658(0.514)	0.286(0.252)	0.000(0.027)	2.15	2.20	2.09
BG ₀ ⁰ (2.5)	–	–	0.036(0.080)	0.417(0.415)	0.520(0.414)	0.027(0.088)	2.50	2.54	2.50
BG ₀ ^{0.43} (2.5)	–	–	0.015(0.068)	0.409(0.428)	0.555(0.425)	0.021(0.076)	2.50	2.58	2.50
BG _{1,0} ^{0.43} (2.5)	0.899(0.670)	0.101(0.318)	0.017(0.073)	0.455(0.426)	0.512(0.435)	0.016(0.065)	2.50	2.53	2.49
BG _{2,0} ^{0.43} (2.5)	0.896(0.721)	0.104(0.267)	0.012(0.080)	0.405(0.418)	0.563(0.440)	0.020(0.060)	2.50	2.59	2.48
BG _{4,0} ^{0.43} (2.5)	0.931(0.622)	0.069(0.364)	0.010(0.084)	0.372(0.443)	0.598(0.409)	0.020(0.063)	2.50	2.63	2.45
BG _{6,0} ^{0.43} (2.5)	0.902(0.690)	0.098(0.304)	0.010(0.087)	0.423(0.457)	0.551(0.392)	0.016(0.062)	2.50	2.57	2.42
BG _{6,0} ^{1.00} (2.5)	0.975(0.735)	0.025(0.263)	0.013(0.071)	0.430(0.465)	0.549(0.417)	0.008(0.046)	2.50	2.55	2.44
BG _{2,6} ^{0.48} (2.7)	0.838(0.517)	0.162(0.475)	0.006(0.041)	0.242(0.336)	0.677(0.507)	0.075(0.115)	2.74	2.82	2.70
BG ₀ ^{0.43} (2.9)	–	–	0.000(0.016)	0.094(0.225)	0.793(0.571)	0.113(0.189)	2.93	3.02	2.93
BG _{2,0} ^{0.43} (2.9)	0.795(0.417)	0.205(0.553)	0.000(0.017)	0.108(0.246)	0.791(0.553)	0.101(0.183)	2.93	2.99	2.90
BG _{3,0} ^{0.43} (2.9)	0.814(0.444)	0.186(0.528)	0.000(0.020)	0.144(0.252)	0.779(0.562)	0.077(0.166)	2.93	2.93	2.87
BG _{4,0} ^{0.43} (2.9)	0.805(0.440)	0.195(0.554)	0.000(0.022)	0.118(0.269)	0.791(0.539)	0.091(0.169)	2.93	2.97	2.86
BG _{6,0} ^{0.43} (2.9)	0.821(0.460)	0.179(0.517)	0.000(0.028)	0.121(0.290)	0.778(0.539)	0.101(0.143)	2.93	2.98	2.80

^aLeft-most entries are $\{x_P^n, x_{Si}^n\}$ data extracted by deconvoluting MAS NMR spectra, as described in detail by Mathew *et al.*^{S1} The values within parentheses are MD-derived populations. The various \overline{N}_{BO}^{Si} data were calculated either from (i) the *nominal* value obtained from the oxide equivalents presented in **Table 1** and *assuming* that the entire phosphate speciation consists of orthophosphate groups [$\overline{N}_{BO}^{Si}(\text{nom})$; see ref. (S1) for details], or from (ii) the $\{x_{Si}^n\}$ set obtained by NMR [$\overline{N}_{BO}^{Si}(\text{NMR})$] or (iii) by MD simulations [$\overline{N}_{BO}^{Si}(\text{MD})$]. While the NMR/MD-derived data generally accord well, we refer to Mathew *et al.*^{S1} for additional information and discussion about the reasons behind the discrepancies in the various $\{x_T^n\}$ and \overline{N}_{BO}^{Si} results. Any deviation to unity for the sum over each MD-derived phosphate $\{x_P^n\}$ or silicate $\{x_{Si}^n\}$ set reflects the presence of minor x_P^0 or x_{Si}^0 populations.

Table S2: Molecular Dynamics Simulation Parameters^a

glass	N_{tot}	N_{Na}	N_{Ca}	N_{P}	N_{Si}	N_{sim}	a/nm^{b}
BG ₀ ⁰ (2.0)	6000	0	1200	0	1200	2	4.309
BG _{2.6} ^{0.48} (2.1)	10017	1718	950	184	1632	2	5.114
BG _{6.0} ^{0.41} (2.1)	6123	928	681	252	829	2	4.336
BG ₀ ⁰ (2.5)	5787	0	963	0	1287	2	4.262
BG ₀ ^{0.43} (2.5)	5516	744	484	0	1144	2	4.196
BG _{1.0} ^{0.43} (2.5)	12279	1686	1097	88	2416	4	5.473
BG _{2.0} ^{0.43} (2.5)	5768	808	524	80	1076	3	4.257
BG _{4.0} ^{0.43} (2.5)	6280	904	588	176	1044	4	4.379
BG _{6.0} ^{0.43} (2.5)	5644	840	544	232	828	2	4.223
BG _{6.0} ^{1.00} (2.5)	6188	1928	0	232	828	2	4.430
BG _{2.6} ^{0.48} (2.7)	9999	1400	771	180	1909	2	5.129
BG ₀ ^{0.43} (2.9)	5606	604	394	0	1304	2	4.238
BG _{2.0} ^{0.43} (2.9)	6080	696	456	88	1272	3	4.347
BG _{3.0} ^{0.43} (2.9)	6081	722	471	126	1205	2	4.350
BG _{4.0} ^{0.43} (2.9)	6372	776	508	176	1192	4	4.414
BG _{6.0} ^{0.43} (2.9)	6000	776	504	240	996	2	4.320

^a N_{tot} represents the total number of atoms in the simulation of one glass model, whereas $\{N_{\text{Na}}, N_{\text{Ca}}, N_{\text{P}}, N_{\text{Si}}\}$ correspond to those of $\{\text{Na}, \text{Ca}, \text{P}, \text{Si}\}$, respectively, and N_{sim} is the number of independent glass models generated.

^bSide length of the cubic box.

Table S3: ^{23}Na NMR parameters^a

glass	$\delta_{\text{Na}}^{\text{CG}}$ (ppm)	fwhm (ppm)	$\bar{\delta}_{\text{Na}}^{\text{iso}}$ (ppm)	$\bar{C}_{Q\eta}$ (MHz)	$W_{\text{Na}}^{\text{iso}}$ (ppm)
BG _{2.6} ^{0.48} (2.1)	-2.5	25.3	8.0	3.50	19.7
BG _{6.0} ^{0.41} (2.1)	-2.9	24.7	7.4	3.51	18.7
BG ₀ ^{0.43} (2.5)	-5.9	26.3	3.6	3.61	20.1
BG _{2.0} ^{0.43} (2.5)	-5.3	25.8	4.2	3.61	19.2
BG _{4.0} ^{0.43} (2.5)	-5.1	25.2	4.2	3.61	18.8
BG _{6.0} ^{0.43} (2.5)	-4.7	24.7	5.1	3.47	18.8
	-18.0 ^b	38.7 ^b	5.0 ^b	3.65 ^b	18.9 ^b
BG _{6.0} ^{1.00} (2.5)	0.9	19.4	9.5	3.42	14.1
BG _{2.6} ^{0.48} (2.7)	-7.2	25.4	2.9	3.57	18.9
BG ₀ ^{0.43} (2.9)	-9.4	25.4	0.2	3.57	19.0
	-22.8 ^b	39.8 ^b	-0.4 ^b	3.60 ^b	20.8 ^b
BG _{2.0} ^{0.43} (2.9)	-8.9	25.2	0.7	3.58	18.8
BG _{4.0} ^{0.43} (2.9)	-8.2	25.1	1.6	3.55	18.8

^aCenter-of-gravity shift ($\delta_{\text{Na}}^{\text{CG}}$; uncertainty ± 0.1 ppm) and full-width at half maximum (fwhm; ± 0.2 ppm) of the ^{23}Na MAS NMR peak recorded at $B_0 = 14.1$ T. The remaining data are best-fit parameters extracted from numerical simulations, assuming a single ^{23}Na site with a Gaussian distribution of isotropic chemical shifts ($\delta_{\text{Na}}^{\text{iso}}$) and a Czjzek distribution^{S26} of quadrupolar products ($C_{Q\eta}$): ^{23}Na average quadrupolar product ($\bar{C}_{Q\eta}$), average isotropic chemical shift ($\bar{\delta}_{\text{Na}}^{\text{iso}}$; ± 1 ppm) and the shift-distribution width ($W_{\text{Na}}^{\text{iso}}$; ± 2 ppm). Owing to the significant $\bar{C}_{Q\eta}/W_{\text{Na}}^{\text{iso}}$ interdependence, where both parameters cause resonance-broadening, the $\bar{C}_{Q\eta}$ -values were first determined by simultaneously fitting the two sets of NMR spectra from BG₀^{0.43}(2.9) and BG_{6.0}^{0.43}(2.5) that were recorded at both 14.1 T and 9.4 T (where the latter field provides more reliable $\bar{C}_{Q\eta}$ -values). We note that the value $\bar{C}_{Q\eta} \approx 1.6$ MHz stated previously in ref. (S3) as representative for the present glasses should be scaled by the factor $\sqrt{5}$.

^bResults obtained at $B_0 = 9.4$ T.

Table S4: MD and NMR Derived Dipolar Second Moments^a

glass	$M_2^{\text{MD}}(\text{Na-P}) - M_2^{\text{NMR}}(\text{Na-P})$ 10^4 Hz^2	$M_2^{\text{MD}}(\text{P-Na}) - M_2^{\text{NMR}}(\text{P-Na})^{\text{b}}$ 10^5 Hz^2	$M_2^{\text{MD}}(\text{Na-Si})$ 10^4 Hz^2	$M_2^{\text{MD}}(\text{Si-Na})^{\text{c}}$ 10^5 Hz^2
BG _{2.6} ^{0.48} (2.1)	2.05±0.15—2.18±0.01	9.57±0.28—9.20±0.12(10.22±0.04)	3.25±0.01	1.71±0.01
BG _{6.0} ^{0.41} (2.1)	4.64±0.07—4.49±0.02	8.54±0.05—7.55±0.10(8.26±0.04)	2.61±0.04	1.46±0.03
BG ₀ ^{0.43} (2.5)	—	—	4.04±0.04	1.31±0.01
BG _{1.0} ^{0.43} (2.5)	0.83±0.39	7.90±0.25	3.81±0.01	1.33±0.01
BG _{2.0} ^{0.43} (2.5)	1.60±0.20—1.59±0.02	8.10±0.05—7.49±0.10(7.86±0.09)	3.56±0.03	1.34±0.01
BG _{4.0} ^{0.43} (2.5)	3.13±0.10—2.95±0.04	8.05±0.10—6.94±0.10(7.68±0.11)	3.13±0.02	1.36±0.01
BG _{6.0} ^{0.43} (2.5)	4.58±0.07—4.36±0.05	8.29±0.33—7.24±0.28(7.99±0.08)	2.67±0.05(2.90±0.04) ^e	1.36±0.03(1.43±0.03—1.49±0.02)
BG _{6.0} ^{1.00} (2.5)	4.01±0.07—5.45±0.01(4.07±0.05) ^d	16.64±0.12—16.91±0.19(22.63±0.04)	2.39±0.03(2.14±0.06) ^e	2.78±0.01(1.90±0.01—2.60±0.03)
BG _{2.6} ^{0.48} (2.7)	2.03±0.16—1.92±0.02	7.90±0.24—7.44±0.10(7.44±0.07)	3.44±0.01	1.26±0.01
BG ₀ ^{0.43} (2.9)	—	—	4.17±0.02	0.97±0.01
BG _{2.0} ^{0.43} (2.9)	1.74±0.19—1.40±0.03	6.86±0.31—6.11±0.10(5.77±0.12)	3.68±0.05	1.01±0.01
BG _{3.0} ^{0.43} (2.9)	2.42±0.14	6.95±0.15	3.47±0.01	1.04±0.01
BG _{4.0} ^{0.43} (2.9)	3.12±0.10—2.79±0.03	6.87±0.09—6.27±0.21(6.23±0.07)	3.25±0.02	1.06±0.01
BG _{6.0} ^{0.43} (2.9)	4.46±0.07	7.21±0.04	2.83±0.03	1.10±0.01

^aDipolar second moments obtained from MD simulations [$M_2^{\text{MD}}(\text{S-I})$] or S{I} REDOR/REAPDOR NMR [$M_2^{\text{NMR}}(\text{S-I})$]. All experimental data were corrected as described by Stevansson *et al.*^{S3}

^bValues in parentheses were calculated from the corresponding $M_2^{\text{NMR}}(\text{Na-P})$ data obtained by $^{23}\text{Na}\{\text{P}\}$ REDOR NMR by using the conversion $M_2(\text{P-Na})=5x_{\text{Na}}M_2(\text{Na-P})/x_{\text{P}}$.^{S3}

^cValues (a—b) in parentheses correspond to directly measured $M_2^{\text{NMR}}(\text{Si-Na})$ data from $^{29}\text{Si}\{^{23}\text{Na}\}$ REAPDOR NMR experiments (left entry), whereas the right entry was derived from the corresponding $^{23}\text{Na}\{^{29}\text{Si}\}$ REDOR NMR data.

^dDerived from the $M_2^{\text{NMR}}(\text{P-Na})$ value of column 3.

^eExperimental $M_2^{\text{NMR}}(\text{Na-Si})$ data in parentheses.

Table S5: Relative Propensities of SiO₄ and PO₄ Groups to Coordinate Na and Ca^a

glass	P	Q _P ⁰	Q _P ¹	Si	Q _{Si} ¹	Q _{Si} ²	Q _{Si} ³	Q _{Si} ⁴
BG _{2.6} ^{0.48} (2.1)	0.93(0.91)	0.89(0.88)	1.14(1.15)	0.94(0.93)	0.75(0.73)	0.94(0.92)	1.21(1.27)	1.48(2.26)
BG _{6.0} ^{0.41} (2.1)	0.96(0.95)	0.92(0.91)	1.20(1.19)	0.90(0.90)	0.72(0.71)	0.90(0.89)	1.12(1.20)	1.65(2.14)
BG ₀ ^{0.43} (2.5)				1.00(1.00)	0.66(0.64)	0.88(0.86)	1.20(1.26)	1.81(2.85)
BG _{1.0} ^{0.43} (2.5)	0.89(0.89)	0.83(0.83)	1.07(1.07)	1.00(1.00)	0.67(0.64)	0.88(0.87)	1.20(1.26)	1.75(2.48)
BG _{2.0} ^{0.43} (2.5)	0.92(0.91)	0.85(0.84)	1.15(1.14)	0.99(0.99)	0.66(0.64)	0.91(0.89)	1.16(1.22)	1.70(2.68)
BG _{4.0} ^{0.43} (2.5)	0.92(0.91)	0.86(0.85)	1.05(1.04)	0.98(0.97)	0.72(0.70)	0.87(0.85)	1.17(1.22)	1.79(2.65)
BG _{6.0} ^{0.43} (2.5)	0.90(0.89)	0.85(0.84)	1.07(1.07)	0.97(0.96)	0.69(0.68)	0.86(0.83)	1.20(1.25)	1.79(2.50)
BG _{2.6} ^{0.48} (2.7)	0.88(0.87)	0.80(0.79)	0.99(0.99)	1.02(1.01)	0.61(0.60)	0.85(0.82)	1.15(1.19)	2.02(3.02)
BG ₀ ^{0.43} (2.9)				1.05(1.05)	0.56(0.54)	0.79(0.76)	1.12(1.13)	1.66(2.58)
BG _{2.0} ^{0.43} (2.9)	0.90(0.90)	0.74(0.74)	1.07(1.08)	1.03(1.04)	0.59(0.57)	0.81(0.78)	1.09(1.12)	1.77(2.62)
BG _{3.0} ^{0.43} (2.9)	0.88(0.87)	0.74(0.73)	1.05(1.03)	1.04(1.04)	0.59(0.57)	0.76(0.74)	1.16(1.18)	1.76(2.52)
BG _{4.0} ^{0.43} (2.9)	0.88(0.88)	0.75(0.74)	1.04(1.02)	1.04(1.04)	0.61(0.59)	0.79(0.77)	1.15(1.17)	1.84(2.70)
BG _{6.0} ^{0.43} (2.9)	0.93(0.89)	0.81(0.81)	1.06(0.98)	1.01(1.02)	0.65(0.59)	0.78(0.77)	1.10(1.16)	1.81(2.72)

^aThe left entries correspond to $R_{\text{Na/Ca}}(Q_T^n) = x_{\text{Ca}}Z(Q_T^n - \text{Na}) / [x_{\text{Na}}Z(Q_T^n - \text{Ca})]$ with $T = \{\text{P, Si}\}$ evaluated for the cutoff radius $r = 450$ pm. Values within parentheses represent $R_{\text{Na/Ca}}(Q_T^n)$ data calculated from coordination numbers derived by requiring *shared* oxygen species between $\{\text{Si, P}\}$ and $\{\text{Na, Ca}\}$, i.e., the values representative for the first coordination shell of the Q_T^n group and plotted in Fig. 7. The labels “P” and “Si” correspond to the net results from the *total* $\{Q_P^n\}$ and $\{Q_{\text{Si}}^n\}$ speciations, respectively. The respective uncertainties (σ) are as follows: P(± 0.05); Q_P^0 (± 0.04); Q_P^1 (± 0.085); Si(± 0.015); Q_{Si}^1 (± 0.05); Q_{Si}^2 (± 0.02); Q_{Si}^3 (± 0.03); Q_{Si}^4 (± 0.15).

Table S6: Parameters for Calculating $M_2(Q_T^n-M)$ ^a

group	$\bar{r}_{T-\text{Na}}$ (pm)	$\bar{r}_{T-\text{Ca}}$ (pm)	$M_2^{\text{FCS}}(Q_T^n-\text{Na})/M_2^{\text{conv}}$	$M_2^{\text{FCS}}(Q_T^n-\text{Ca})/M_2^{\text{conv}}$
Q_{P}^0	324	345	0.92(0.016)	0.92(0.028)
Q_{P}^1	328	352	0.90(0.034)	0.86(0.055)
Q_{Si}^1	325	344	0.90(0.016)	0.92(0.038)
Q_{Si}^2	330	349	0.87(0.020)	0.86(0.046)
Q_{Si}^3	336	354	0.81(0.014)	0.73(0.049)
Q_{Si}^4	343	371	0.73(0.036)	0.39(0.096)

^aAverage distance from the central atom (Si or P) of the Q_T^n moiety to each of Na and Ca in the first coordination sphere (FCS) of the Q_T^n group, i.e., second coordination sphere of Si and P. The ratio $M_2^{\text{FCS}}(Q_T^n-\text{Na})/M_2^{\text{conv}}$ represents the fraction of the *converged* dipolar second moment that the FCS accounts for. The data are presented as $M(S)$, with M being the average value across the set of 13 mixed-modifier glasses (see **Table 1**). The span S corresponds to the difference between the extreme values observed for the given Q_T^n group among the glasses.

Table S7: Distribution of Na and Ca around BO/NBO Sites in Soda-Lime-Silicate Glasses^a

glass	$x(\text{NBO-Na})$	$x(\text{NBO-Ca})$	$x(\text{NBO-Na/Ca})$	$Z(\text{NBO-}M_{\text{tot}})$
BG ₀ ^{0.43} (2.5)	0.096(0.229)	0.135(0.072)	0.769(0.699)	3.07
BG ₀ ^{0.43} (2.9)	0.109(0.267)	0.177(0.096)	0.712(0.635)	2.74
	0.222 ^b	0.061 ^b	0.716 ^b	
BG ₀ ^{0.5} (2.67) ^c	0.145(0.319)	0.093(0.049)	0.762(0.632)	
BG ₀ ^{0.5} (3.33) ^d	0.128(0.326)	—	—	
	0.296 ^e	0.037 ^e	0.667 ^e	
glass ^f	$x(\text{BO-Na})$	$x(\text{BO-Ca})$	$x(\text{BO-Na/Ca})$	$Z(\text{BO-}M_{\text{tot}})$
BG ₀ ^{0.43} (2.5)	0.645(0.440)	0.126(0.252)	0.127(0.206)	1.35
BG ₀ ^{0.43} (2.9)	0.572(0.407)	0.125(0.247)	0.067(0.109)	1.00
	0.606 ^g	0.394 ^g	0	
BG ₀ ^{0.5} (2.67) ^c	0.710(0.516)	0.111(0.211)	0.087(0.181)	
	0.667 ^h	0.333 ^h	0	

^aMD-derived fractional populations $x(X\text{-Na})$, $x(X\text{-Ca})$, and $x(X\text{-Na/Ca})$ for $X = \{\text{BO}, \text{NBO}\}$. The uncertainties of each BO/NBO population of BG₀^{0.43}(2.5) or BG₀^{0.43}(2.9) is ± 0.01 throughout. The NBO and BO average total coordination numbers with respect to *both* Na and Ca are listed in the rightmost column. However, $Z_{\text{tot}} \equiv Z(X\text{-}M_{\text{tot}})$ varies among different $X=\text{NBO}$ or $X=\text{BO}$ sites in the structure and this distribution also depends on the glass composition. Values within parentheses correspond to the respective populations obtained from a random Na/Ca partitioning for the given fraction $q = n(\text{Na}_2\text{O})/[n(\text{Na}_2\text{O}) + n(\text{CaO})]$ of the BG_p^q($\overline{N}_{\text{BO}}^{\text{Si}}$) glass; they were obtained as a weighted average over a set of binomial distributions $\{B(\mathcal{Z}, q)\}$ (see Pedone *et al.*^{S27}). Here the total coordination number \mathcal{Z}_j of the oxygen site j relates to Z_{tot} as $Z_{\text{tot}} = \sum_j y_j \mathcal{Z}_j$ with $\sum_j y_j = 1$.

^bPopulations obtained from a single binomial distribution $B(\mathcal{Z}, q) = \mathcal{Z}![p!(\mathcal{Z} - p)!]^{-1}A^p(1 - A)^{\mathcal{Z}-p}$ with $A = 2q/(1 + q)$, $\mathcal{Z} = 3$, and $q = 0.43$.

^cData taken from Pedone *et al.*^{S27}

^dData obtained by Lee and Stebbins from analysis of ¹⁷O MAS NMR spectra.^{S24} An independent 3QMAS ¹⁷O NMR-derived estimate resulted in $x(\text{NBO-Na})=0.182$. The value in parentheses corresponds to the prediction from a binomial distribution with $\mathcal{Z} = 3$ and $q = 0.5$;^{S24} for unknown reasons, this value deviates slightly from that obtained by us (0.296).

^eAs in **b**, with $\mathcal{Z} = 3$ and $q = 0.5$.

^fThe fractional populations do not sum to unity because some BO sites do not coordinate to *any* network-modifier; these fractions amount to 0.102, 0.236, and 0.092 for the BG₀^{0.43}(2.5), BG₀^{0.43}(2.9), and BG₀^{0.5}(2.67) structures.

^gAs in **b**, with $\mathcal{Z} = 1$ and $q = 0.43$.

^hAs in **b**, with $\mathcal{Z} = 1$ and $q = 0.5$.

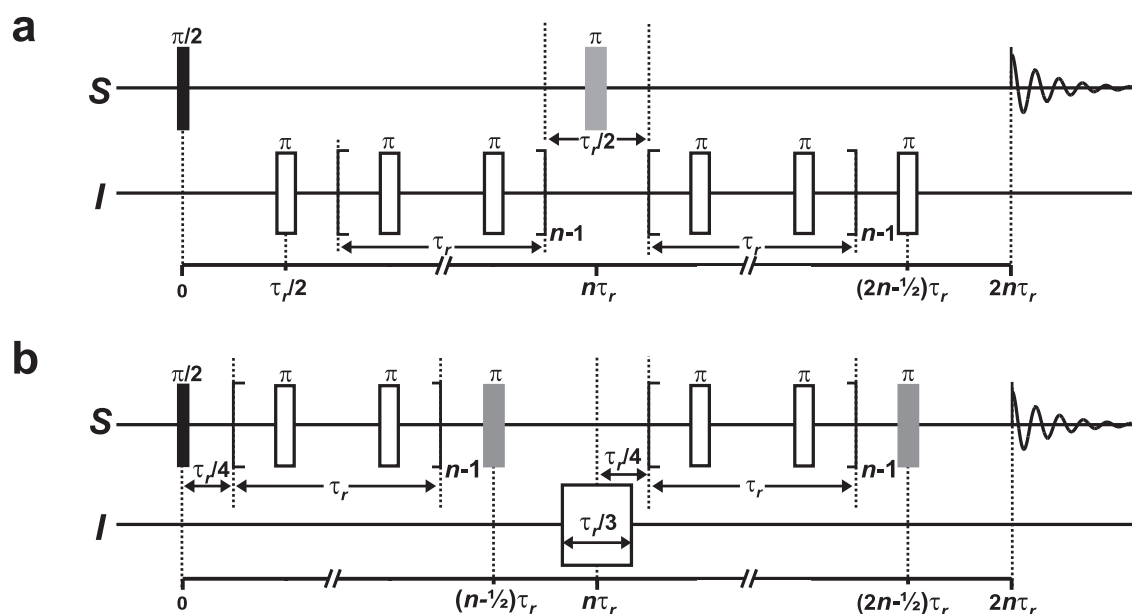


Figure S1. Radio-frequency (rf) pulse schemes utilized for acquiring the (a) $^{23}\text{Na}\{^{29}\text{Si}\}$ and $^{23}\text{Na}\{^{31}\text{P}\}$ REDOR,^{S28,S29} and (b) $^{29}\text{Si}\{^{23}\text{Na}\}$ and $^{31}\text{P}\{^{23}\text{Na}\}$ REAPDOR^{S30} NMR data. For spin-pairs involving a quadrupolar nucleus (here the spin-3/2 ^{23}Na), coupled to a spin-1/2 $I=\{^{31}\text{P}, ^{29}\text{Si}\}$ species, one must ensure that the recoupling pulses are applied to the latter for avoiding a severely compromised recoupling performance and NMR signal losses.^{S3,S30} Solid black rectangles and open/gray rectangles represent $\pi/2$ and π -pulses, respectively. The gray rectangles mark pulses with fixed positions, regardless of the choice of the duration of the recoupling period; they are responsible for refocusing S-spin isotropic chemical shifts. The number of recoupling π -pulses (open rectangles) is incremented in blocks of 4 pulses that together span two rotational periods. This is commensurate with $\tau_{\text{rec}} = 2n\tau_r$ and $n = 1, 2, 3, \dots$. The reference signal $S_0(\tau_{\text{rec}})$ in (a) is recorded by leaving out all I-spin recoupling pulses, whereas $S_0(\tau_{\text{rec}})$ in (b) results by only omitting the I-spin adiabatic-passage pulse.

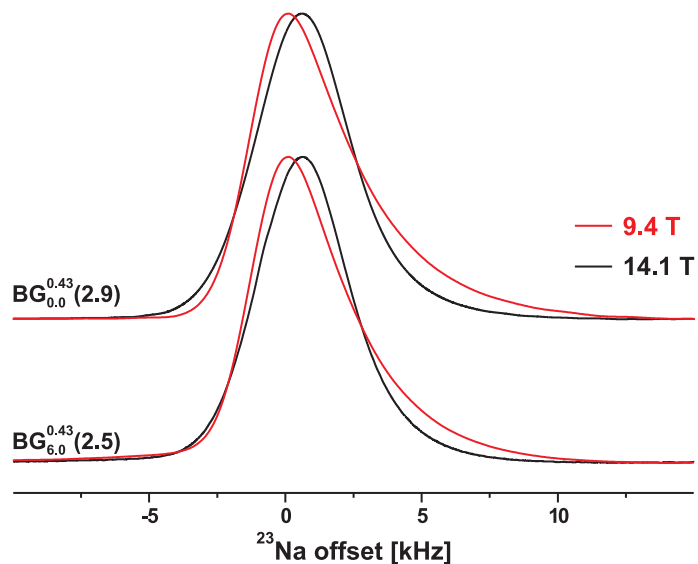


Figure S2. ^{23}Na MAS spectra recorded at external fields of $B_0=9.4$ T and $B_0=14.1$ T at the MAS rates of 14.0 and 24.0 kHz, respectively. Note the very similar fwhm peak-widths observed from each glass at both B_0 values, indicating that the emphasized second-order quadrupolar peak-broadening (that scales as B_0^{-1}) resulting at the lower field is counterbalanced nearly exactly by the reduced chemical-shift dispersion (scaling linearly with B_0). The main distinctions among the NMR spectra are manifested in their shifted peak-maxima and the more pronounced tail towards lower ppm-values observed at $B_0=9.4$ T, both stemming from the larger second-order quadrupolar effects at the lower field.

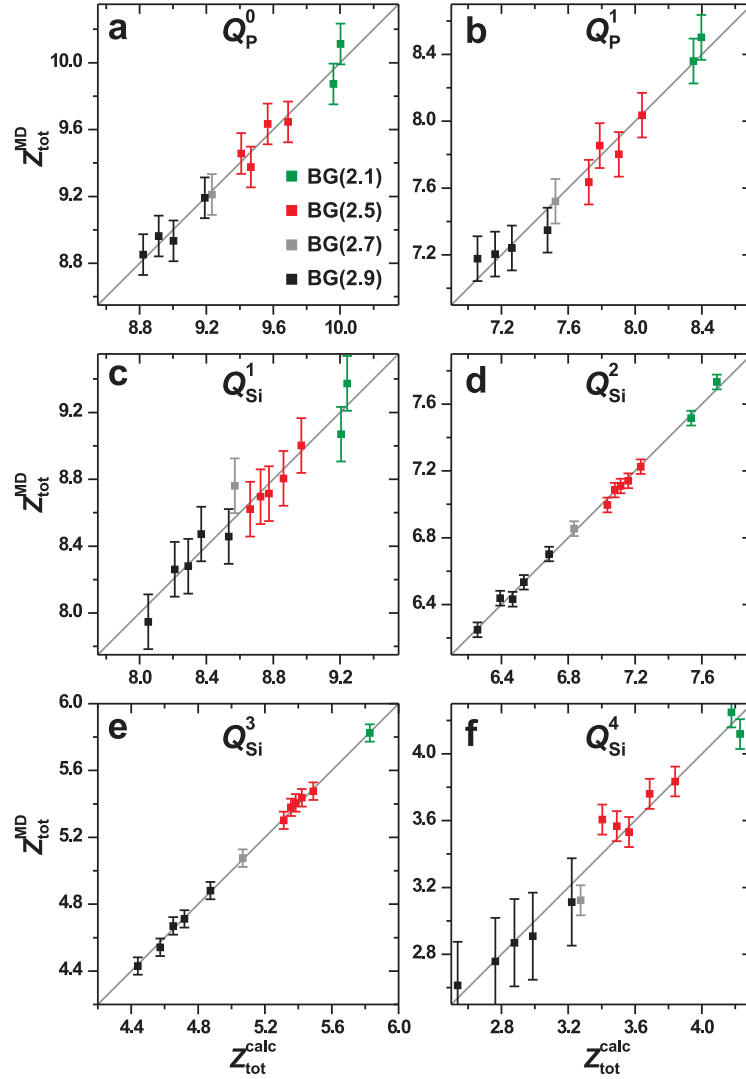


Figure S3. Correlation between the MD-derived total coordination number $Z_{\text{tot}}^{\text{MD}}$ and its modeled counterpart $Z_{\text{tot}}^{\text{calc}}$ calculated from eqs. (S1)–(S6) for the as-indicated Q_T^n groups. Each straight line of unity slope marks the ideal correlation.

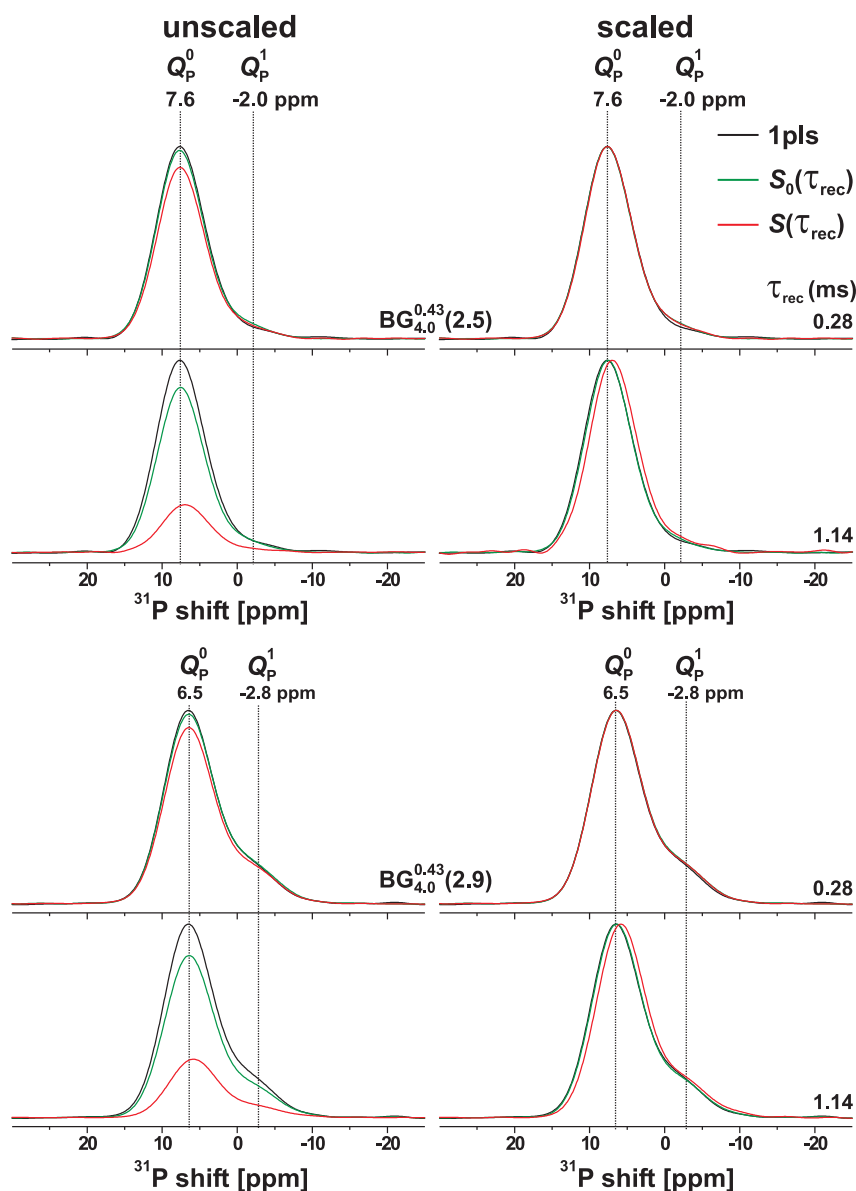


Figure S4. ^{31}P MAS NMR spectra recorded either by direct excitation using single pulses (“1pls”) or by $^{31}\text{P}\{^{23}\text{Na}\}$ NMR REAPDOR, where $S(\tau_{\text{rec}})$ and $S_0(\tau_{\text{rec}})$ represents the spectrum obtained in the *presence* and *absence* of dipolar dephasing, respectively (see Fig. S1). Data from two dephasing periods of $\tau_{\text{rec}} = 0.28$ ms and $\tau_{\text{rec}} = 1.14$ ms are displayed for each as-indicated $\text{BG}_{4.0}^g(\overline{N}_{\text{BO}}^{\text{Si}})$ specimen, with the left and right columns presenting NMR spectra using absolute and relative NMR peak intensities, respectively. The NMR peak positions from the Q_{P}^0 and Q_{P}^1 groups are indicated. All phosphate moieties exhibit an overall similar dipolar dephasing: this effect stems from a slightly larger coordination number $Z_{\text{Na}}(Q_{\text{P}}^0)$ of the Q_{P}^0 groups compared with that of the Q_{P}^1 groups, $Z_{\text{Na}}(Q_{\text{P}}^1)$ (see Fig. 9), *despite* that the latter displays a higher *preference* for contacts with Na relative to Ca. The resulting (slightly) higher dipolar second moment $M_2(Q_{\text{P}}^0\text{-Na})$ is reflected in the depleted NMR signal intensity at high ppm-values and an accompanying NMR peak-displacement of the ^{31}P NMR signal from Q_{P}^0 groups towards lower shifts in the REAPDOR-dephased NMR spectrum [$S(\tau_{\text{rec}})$] relative to its “reference” counterpart [$S_0(\tau_{\text{rec}})$]. This trend is observed for both BG specimens.

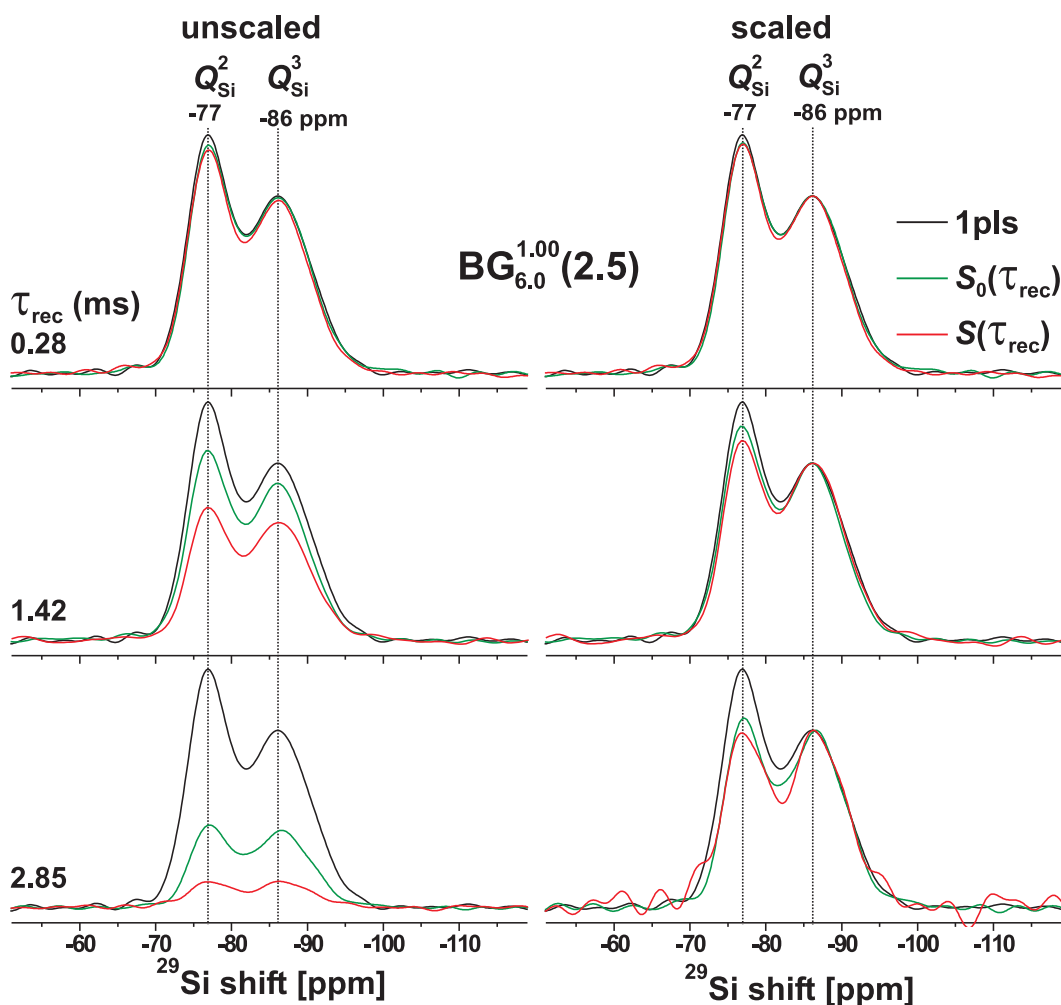


Figure S5. ^{29}Si MAS NMR spectra recorded from the $\text{BG}_{6.0}^{1.00}(2.5)$ glass, either by using single pulses (“1pls”) or $^{29}\text{Si}\{^{23}\text{Na}\}$ REAPDOR NMR with increasing dephasing intervals τ_{rec} . All spectra reveal two main ^{29}Si NMR signals from Q_{Si}^2 and Q_{Si}^3 structural moieties. The higher dipolar dephasing observed from the Q_{Si}^2 groups compared with their Q_{Si}^3 counterparts is consistent with $Z_{\text{Na}}(Q_{\text{Si}}^2) > Z_{\text{Na}}(Q_{\text{Si}}^3)$, despite the stronger (relative) preference for the Q_{Si}^3 moieties to coordinate Na rather than Ca (see Fig. 9 and Table S5). Note that the differences between the black and green curves stem from T_2 relaxation effects and rf-pulse imperfections, while the differences between the green and red curves faithfully reflect the various distinct Q_{Si}^n –Na contacts.

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